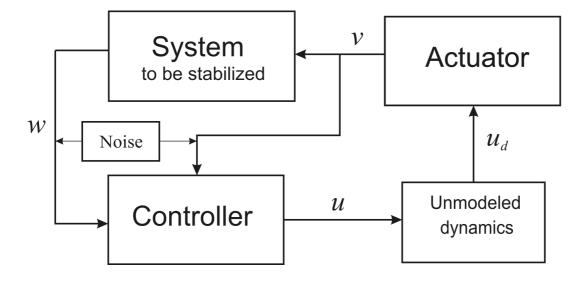
Problem 15

The system is composed of a linear system to be stabilized, a non-linear actuator and some fast stable unmodeled dynamics of the actuator. The general detailed problem description is singled out.



1. The system to be stabilized: $\dot{w} = Aw + Bv$, $w \in \mathbb{R}^3, v \in \mathbb{R}$ is the input,

$$A = \begin{pmatrix} 1 & -1 & -1 \\ 0 & -2 & 1 \\ 1 & 0 & 1 \end{pmatrix}, \quad B = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}.$$

2. The actuator output is defined as $v = x_1$, where the actuator equations are

$$\dot{x}_1 = -\sin(0.7 t - 5) + 0.5 \cos 2t + 2 x_2,$$

$$\dot{x}_2 = a(x_1, x_2, x_3, t) + (2 - \cos x_1) u_d,$$

$$\dot{x}_3 = \cos(2x_1 - x_3 + t) - 2 x_3 + 0.3 u_d.$$

3. The "unmodeled" (singular) dynamics (actually a part of the actuator) is for the simulation presented by the equation

4. a(x,t) represents the system uncertainty. For a single student (I) and for a pair of students (II): for both $a = \cos (1 - 2 x_3)$ and $a = \cos (1 + 2 x_3)$ the same controller is to provide for the exact actuator tracking of the two command signals

$$v_c(t) = \sin(1.3 t + 1) - 0.8 \cos(0.9 t - 5),$$

$$v_c(t) = -2 \sin(2 t) + \cos(t - 1) + 0.01 \cos 10t.$$
(1)

בהצלחה!