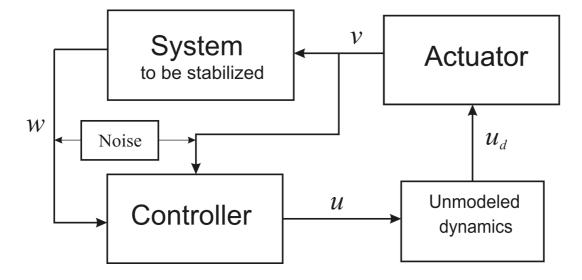
## Problem 13

The system is composed of a linear system to be stabilized, a non-linear actuator and some fast stable unmodeled dynamics of the actuator. The general detailed problem description is singled out.



1. The system to be stabilized:  $\dot{w} = Aw + Bv$ ,  $w \in \mathbb{R}^3, v \in \mathbb{R}$  is the input,

$$A = \begin{pmatrix} 1 & 1 & 0 \\ 0 & -1 & -1 \\ 1 & 0 & 1 \end{pmatrix}, \quad B = \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix}.$$

2. The actuator output is defined as  $v = x_1$ , where the actuator equations are

$$\dot{x}_1 = -\sin(0.8 t + 5) - 0.5 \cos t - 2 x_2,$$
  
$$\dot{x}_2 = a(x_1, x_2, x_3, t) + (1 - 0.6 \cos(x_1 + x_3 + 7)) u_d,$$
  
$$\dot{x}_3 = \cos(x_1 - 0.7 x_3 - t) - 2 x_3 + 0.4 u_d.$$

3. The "unmodeled" (singular) dynamics (actually a part of the actuator) is for the simulation presented by the equation

$$\ddot{u}_d = -2\varepsilon^{-1}\ddot{u}_d - 4\varepsilon^{-2}\dot{u}_d - 5\varepsilon^{-3}(u_d - u).$$

4. a(x,t) represents the system uncertainty. For a single student (I) and for a pair of students (II): for both  $a = cos(1 - 3 x_3)$  and  $a = cos(1 + 3 x_3)$  the same controller is to provide for the exact actuator tracking of the two command signals

$$v_c(t) = \sin (2 t + 1) - 0.8 \cos (t - 5),$$

$$v_c(t) = -\sin (2 t) + 0.5 \cos (t - 1) + 0.01 \cos 10t.$$
(1)

## בהצלחה!