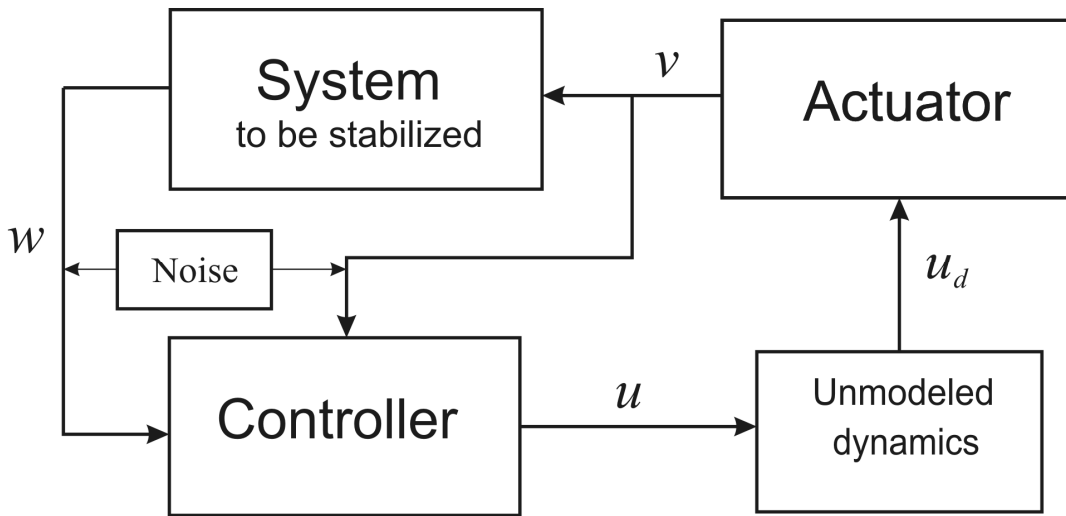


Problem 2

The system is composed of a linear system to be stabilized, a non-linear actuator and some fast stable unmodeled dynamics of the actuator. The general detailed problem description is singled out.



1. The system to be stabilized: $\dot{w} = Aw + Bv$, $w \in \mathbb{R}^3, v \in \mathbb{R}$ is the input,

$$A = \begin{pmatrix} 1 & 1 & 2 \\ 1 & 2 & 3 \\ 1 & 2 & 0 \end{pmatrix}, \quad B = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}.$$

2. The actuator output is defined as $v = x_1$, where the actuator equations are

$$\dot{x}_1 = \sin t - \cos 2t - x_2,$$

$$\dot{x}_2 = a(x_1, x_2, x_3, t) - (2 + \cos(1 + x_3)) u_d,$$

$$\dot{x}_3 = \cos(2x_1 - x_3 + 2t) - 2x_3 - 0.5 u_d.$$

3. The “unmodeled” (singular) dynamics (actually a part of the actuator) is for the simulation presented by the equation

$$\ddot{u}_d = -\varepsilon^{-1} \ddot{u}_d - 2\varepsilon^{-2} \dot{u}_d - \varepsilon^{-3} (u_d - u).$$

4. $a(x, t)$ represents the system uncertainty. **For a single student (I) and for a pair of students (II):** for both $a = \cos(x_1 + 2x_3)$ and $a = \cos(x_1 - 2x_3)$ the same controller is to provide for the exact actuator tracking of the two command signals

$$v_c(t) = \cos 2t + \sin t - 1, \tag{1}$$

$$v_c(t) = \sin t - 0.5 \cos 2t - 0.01 \cos 20t.$$

בהצלחה!