Abelian varieties over ample fields of positive characteristic

(Joint work with Arno Fehm)

A field K is called ample, if every smooth curve C/K satisfies $C(K)=\emptyset$ or $|C(K)|=\infty$.

Theorem. Let A be a non-zero abelian variety over an ample field K. Then the rank of the abelian group A(K) is infinite.

In the special case $\operatorname{char}(K)=0$ we established this Theorem about one year ago. Now we can prove it in the (more complicated) case $\operatorname{char}(K)>0$ as well, making use of work of Ghioca and Moosa and of Kim on the Mordell-Lang conjecture in positive characteristic.